

Heating, ventilation, and air conditioning

Purdue ME 597, Distributed Energy Resources

Kevin J. Kircher

Outline

Heating with electricity

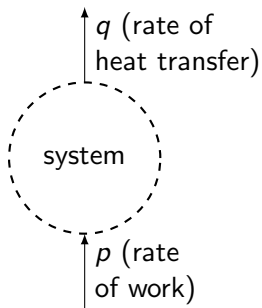
Air conditioning

Sizing heating and cooling equipment

Common HVAC system configurations

Thermal distribution models

Electric resistance heating

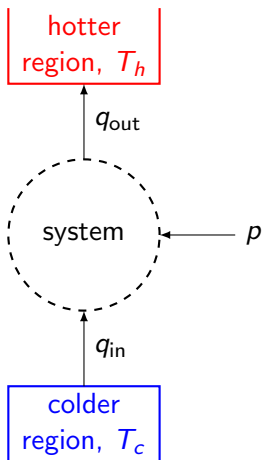


- (steady-state) 1st law: $p = q$
- coefficient of performance:

$$\eta = \frac{\text{heat transfer output}}{\text{net work input}} = \frac{q}{p} = 1$$

- Joule heating: $p = I^2 R$
- dirt-cheap to install, lasts \sim forever
- but inefficient/expensive to run

Heat pump thermodynamic cycles



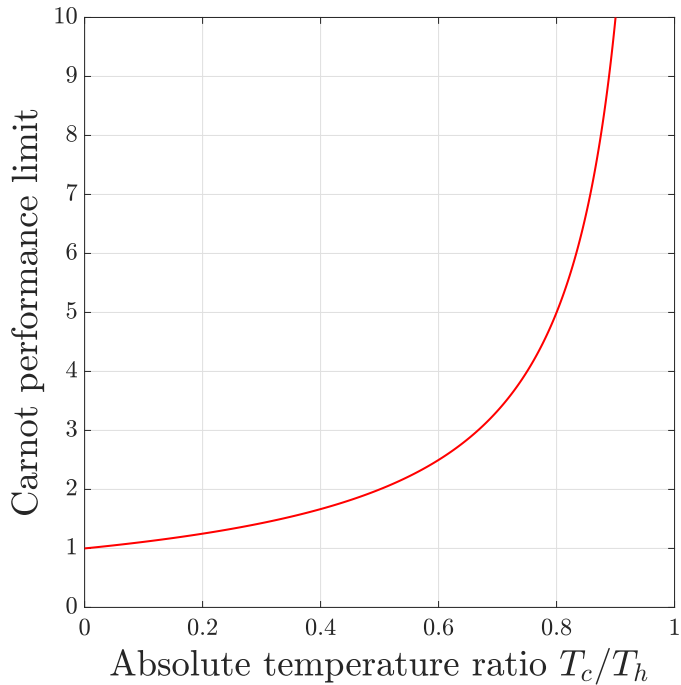
- 1st law: $q_{in} + p = q_{out}$
- heating capacity: q_{out}
- coefficient of performance:

$$\begin{aligned}\eta &= \frac{\text{heat transfer output}}{\text{net work input}} \\ &= \frac{q_{out}}{p} = \frac{q_{out}}{q_{out} - q_{in}} \\ &= \frac{1}{1 - q_{in}/q_{out}}\end{aligned}$$

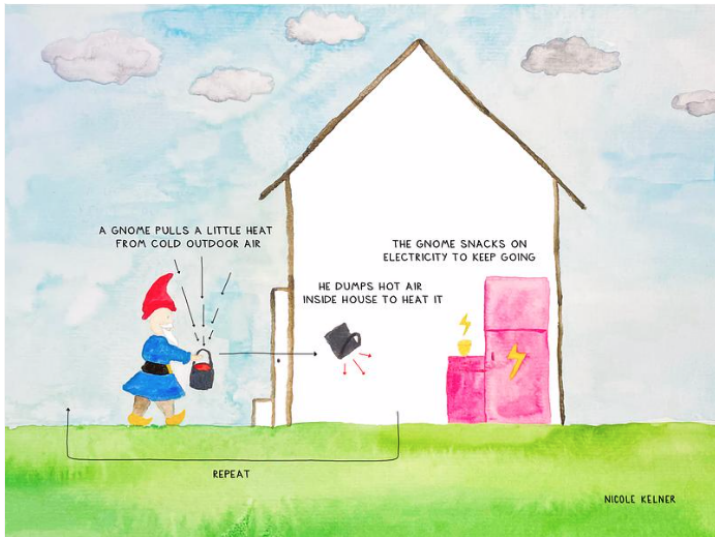
- Carnot performance limit:

$$\eta \leq \frac{1}{1 - T_c/T_h}$$

with T_c , T_h in Kelvin



How to pump heat

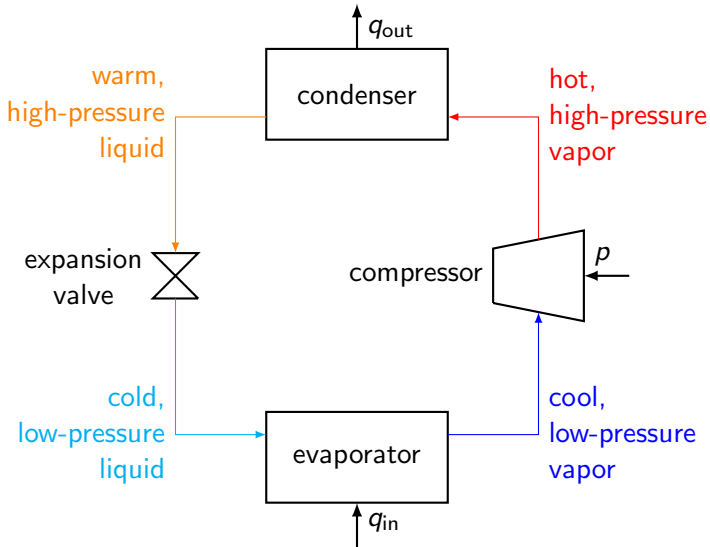


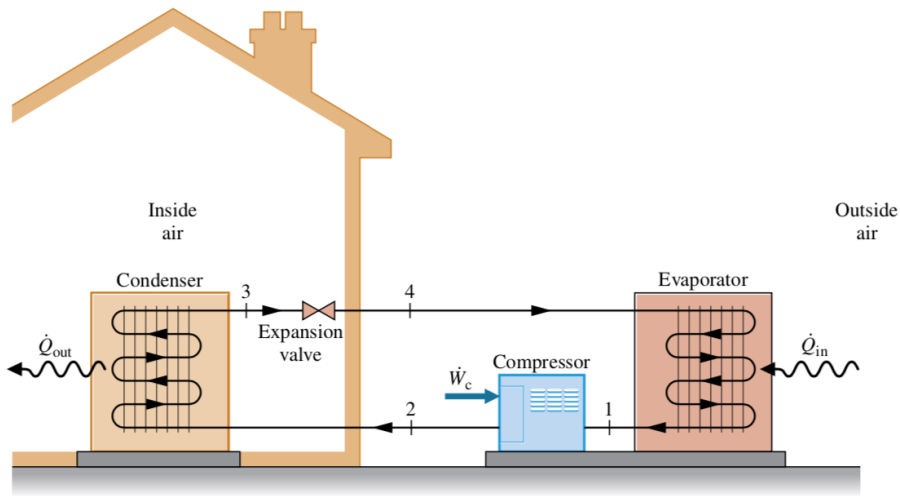
How to pump heat



MANUAL HEAT PUMPS ARE SUCH A PAIN.

How to pump heat (vapor compression cycle)

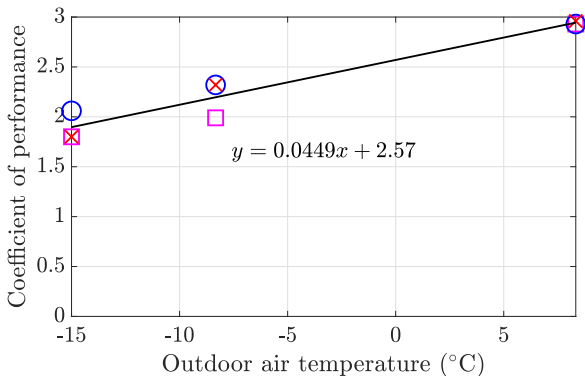




Moran (2018): *Fundamentals of Engineering Thermodynamics*

Fitting real heat pump COPs to manufacturer data

- real heat pumps COPs don't come close to Carnot limit
- NEEP **collects** manufacturer-reported steady-state COP data



central ducted units from 3 manufacturers, 21 °C indoor air

Simple heat pump simulation

- assume \sim constant indoor temperature
- model COP as a function \sim only of outdoor temperature θ
- fit COP curve $\eta : \mathbf{R} \rightarrow \mathbf{R}$ to manufacturer data, such as

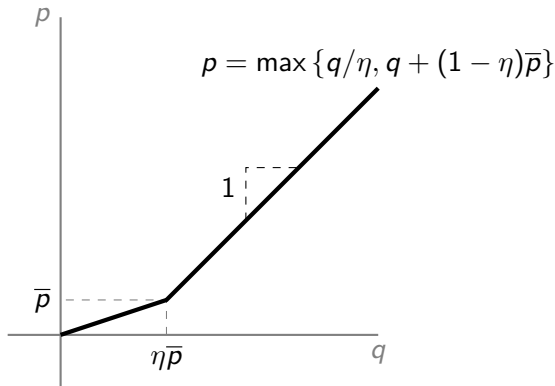
$$\eta(\theta) = \max\{1, 0.0449\theta + 2.57\}$$

(most heat pumps switch to resistance [COP 1] at low θ)

- read off cold-weather compressor power limit \bar{p} from data
- simulate building with constraint $q(t) \in [0, \eta(\theta(t))\bar{p}]$
- set input electric power to $p(t) = q(t)/\eta(\theta(t))$

Heat pumps with resistance backup

- heat pumps are expensive to install but cheap to run
- resistance is cheap to install but expensive to run
- hybrid systems pair heat pumps with resistance backup



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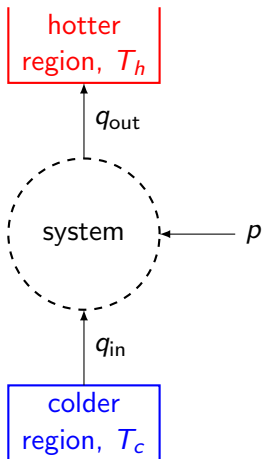
Air conditioners are just one-way heat pumps

- most heat pumps can run in reverse to cool and dehumidify
⇒ lower up-front cost than heater + (one-way) air conditioner

Heat pump vocabulary

| heat source | heat sink | device name |
|------------------|--------------|--|
| refrigerator air | kitchen air | refrigerator |
| freezer air | kitchen air | freezer |
| outdoor air | indoor air | air-source heat pump (ASHP) (or air-to-air heat pump) |
| indoor air | outdoor air | air conditioner or ASHP |
| outdoor ground | indoor air | ground-source heat pump (or geothermal heat pump) |
| outdoor air | indoor water | heat-pump water heater |
| indoor air | indoor water | heat-pump water heater |
| indoor water | outdoor air | chiller |
| outdoor water | indoor air | water-source heat pump |

Refrigeration thermodynamic cycles



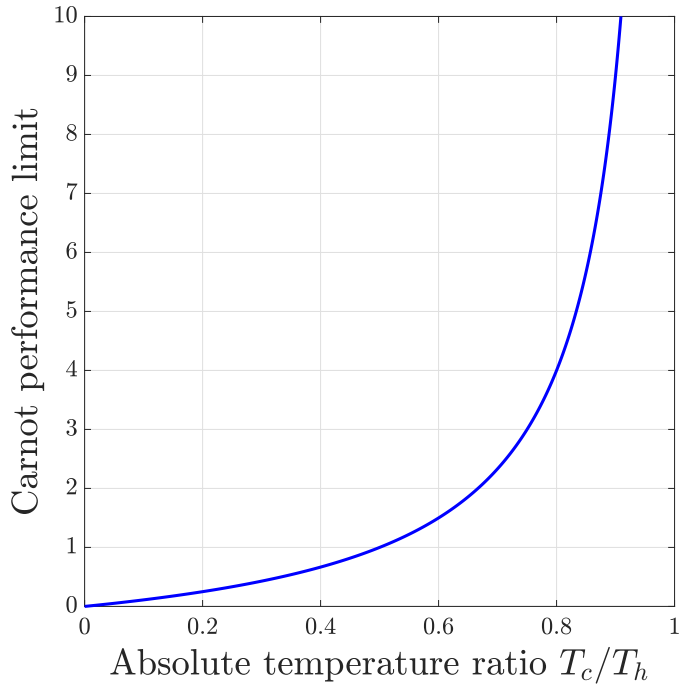
- 1st law: $q_{in} + p = q_{out}$
- coefficient of performance:

$$\begin{aligned}\eta &= \frac{\text{heat transfer **input**}}{\text{net work input}} \\ &= \frac{q_{in}}{p} = \frac{q_{in}}{q_{out} - q_{in}} \\ &= \frac{q_{in}/q_{out}}{1 - q_{in}/q_{out}}\end{aligned}$$

- Carnot performance limit:

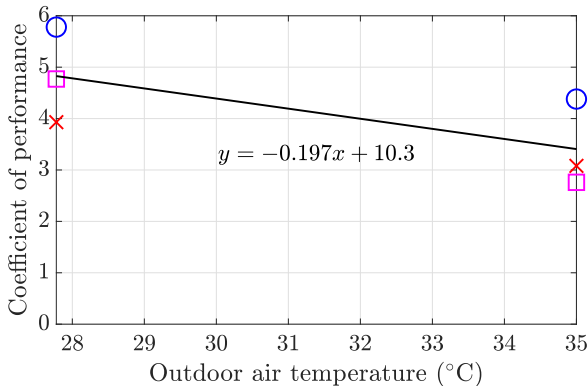
$$\eta \leq \frac{T_c/T_h}{1 - T_c/T_h}$$

with T_c , T_h in Kelvin



Real air conditioner COPs

NEEP [database](#) also has cooling COP data



central ducted units from 3 manufacturers, 21 °C indoor air

Dehumidification

- air conditioners
 - ◇ reduce indoor air temperature (**sensible** load)
 - ◇ condense water out of indoor air (**latent** load)
- total load = sensible load + latent load
- **sensible heat ratio** s is ratio of sensible load to total load
- building simulations often produce sensible load $q(t)$ only
- to account for dehumidification, estimate s and set

$$p(t) = \frac{q_{\text{tot}}(t)}{\eta(\theta(t))} = \frac{q(t)}{s\eta(\theta(t))}$$

- in reality, s depends on weather, building, occupant behavior
- first cut: set $s \approx 70$ to 95% for humid to dry climates

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Sizing for heating

- estimate overall indoor-outdoor thermal resistance R
- get design outdoor temperature θ^{des}
- set design indoor temperature T^{des} to occupant preference
- pick plausible q_e^{des} for ~ 4 AM
- size to steady-state heat load in design conditions:

$$\bar{p}_h = \frac{r}{\eta(\theta^{\text{des}})} \left(\frac{T^{\text{des}} - \theta^{\text{des}}}{R} - q_e^{\text{des}} \right)$$

- oversize ratio $r \approx 1.2$ to 1.5 , typically

Sizing for cooling

- like heating, but

$$\bar{p}_c = \frac{r}{s\eta(\theta^{\text{des}})} \left(\frac{\theta^{\text{des}} - T^{\text{des}}}{R} + q_e^{\text{des}} \right)$$

- q_e^{des} should be plausible for sunny afternoon

Sizing two-way heat pumps

- calculate \bar{p}_h and \bar{p}_c for heating and cooling design conditions
- if $\bar{p}_h \leq \bar{p}_c$, set $\bar{p} = \bar{p}_c$ (size for cooling)
- if $\bar{p}_h > \bar{p}_c$, options:
 1. set $\bar{p} = \bar{p}_h$ (size for heating)
 2. set $\bar{p} = \bar{p}_c$ and add backup $\geq \eta(\theta^{\text{des}})(\bar{p}_h - \bar{p})$
 3. get biggest available unit and add backup $\geq \eta(\theta^{\text{des}})(\bar{p}_h - \bar{p})$
- backup heat could be
 - ◇ another heat pump
 - ◇ resistance
 - ◇ heat storage
 - ◇ wood
 - ◇ propane
 - ◇ heating oil
 - ◇ natural gas

Sizing example for a house in Lafayette

| | θ^{des} ($^{\circ}\text{C}$) | T^{des} ($^{\circ}\text{C}$) | q_e^{des} (kW) | $\eta(\theta^{\text{des}})$ |
|---------|--|---|-------------------------|-----------------------------|
| heating | -16 | 21 | 1 | 1.8 |
| cooling | 32 | 24 | 4 | 4 |

- input parameters: $R = 3$ $^{\circ}\text{C}/\text{kW}$, $r = 1.3$, $s = 0.8$
- sizing results: $\bar{p}_h = 8.2$ kW, $\bar{p}_c = 2.7$ kW
- biggest available residential heat pumps have $\bar{p} \approx 7.5$ kW

\implies need some form of backup heat

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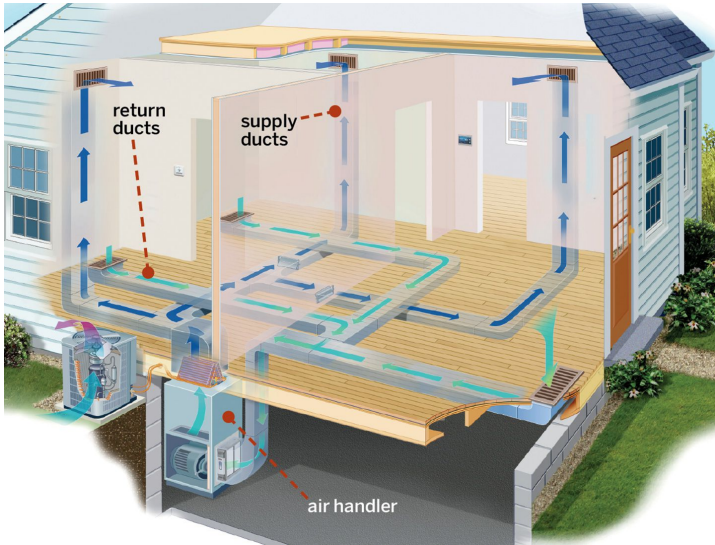
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Central ducted residential systems



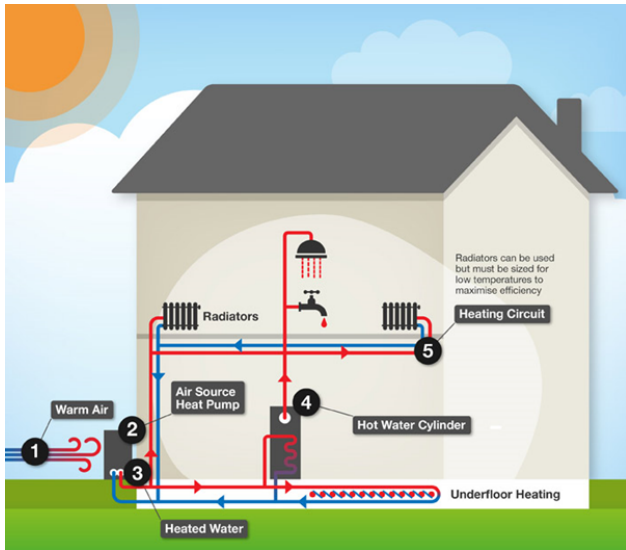
This Old House: Central air conditioning

Ductless mini-split residential systems

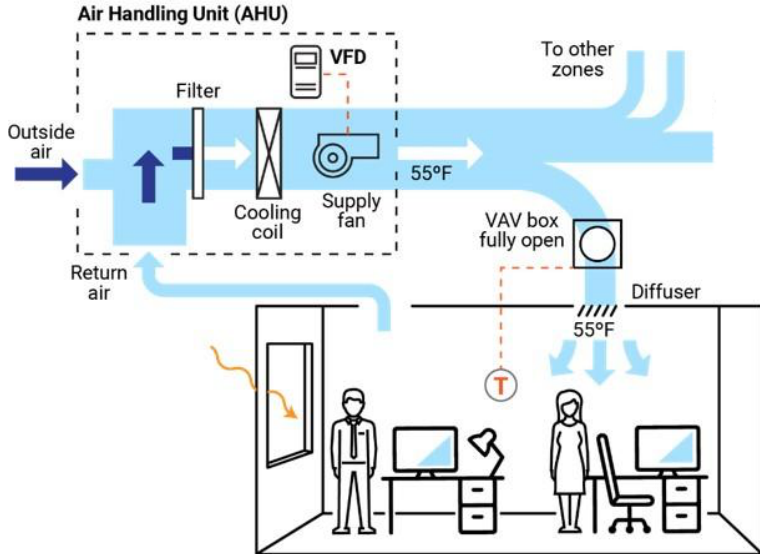


New Hampshire Electric Co-Op: [Ductless mini-split heat pumps](#)

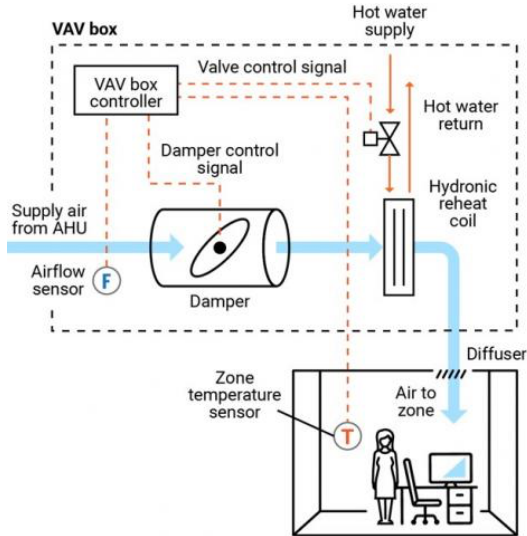
Hydronic residential systems



Variable air volume commercial systems



Variable air volume boxes



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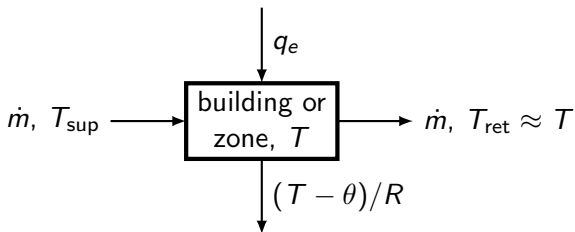
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Forced-air heat transfer

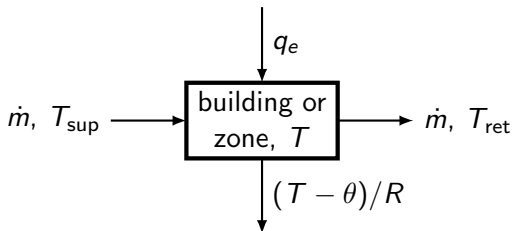


- $\dot{m}(t)$ (kg/s) is mass flow rate of supply air
- power balance:

$$C \frac{dT(t)}{dt} = \frac{\theta(t) - T(t)}{R} + \underbrace{\dot{m}(t)c_p(T_{\text{sup}}(t) - T(t))}_{q_c(t)} + q_e(t)$$

- $c_p = 1 \text{ kJ}/(\text{kg}^\circ\text{C})$ is specific heat of air at constant pressure

Hydronic heat transfer

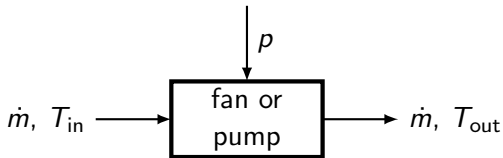


- $\dot{m}(t)$ (kg/s) is mass flow rate of supply water
- power balance:

$$C \frac{dT(t)}{dt} = \frac{\theta(t) - T(t)}{R} + \underbrace{\dot{m}(t)c(T_{\text{sup}}(t) - T_{\text{ret}}(t))}_{q_c(t)} + q_e(t)$$

- $c = 4.2 \text{ kJ}/(\text{kg}^\circ\text{C})$ is specific heat of water

Fans and pumps



- (rough) fan power balance:

$$p(t) \approx \dot{m}(t)c_p(T_{out}(t) - T_{in}(t))$$

- pump:

$$p(t) \approx \dot{m}(t) \left[c(T_{out}(t) - T_{in}(t)) + \frac{P_{out}(t) - P_{in}(t)}{\rho} \right]$$

- $P_{in}(t), P_{out}(t)$ (kPa) are inlet, outlet pressures
- $\rho = 1000 \text{ kg/m}^3$ is density of water

Pump and fan affinity laws

- in theory, pumps and fans follow the affinity law

$$p(t) = \alpha \dot{m}(t)^3$$

where $\alpha = p_{\text{rated}} / \dot{m}_{\text{rated}}^3$

- in practice, usually fit a model to (\dot{m}, p) data, such as

$$p(t) = \beta_0 + \beta_1 \dot{m}(t) + \beta_2 \dot{m}(t)^2 + \beta_3 \dot{m}(t)^3$$